

# Probabilistic Programming with Lea

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PROB  
PROG  
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## Lea in a nutshell...

- **PP library for Python** 2.6+ and 3.x
- **Discrete probabilities only** – support: numbers, strings, times, ...
- **Comprehensive toolkit** – CPT, BN, JPD, Markov chains, probabilistic arithmetic, standard indicators, information theory, random sampling, plotting, etc.
- **Open probability representation** – float, fraction, decimal
- **Symbolic computation** – enableable by [SymPy library](#)
- **Exact algorithm**, by default – new “[Statutes](#)” algorithm
- **Approximate algorithms**, if needed – rejection sampling, likelihood weighting
- **Machine learning** – maximum likelihood, EM algorithms
- **Easy!** – comprehensive Wiki [tutorials](#) & [examples](#) / Jupyter notebooks
- **Open-source** – LGPL license – Find Lea on [Git repo](#) & [PyPI](#)



Lea 3

Check out online  
[Lea playground](#)

## Open probability representation

from fractions...

```
>>> flipA = bernoulli('1/2')
>>> flipB = bernoulli('1/4')
>>> flips = flipA + flipB
>>> flips
0 : 3/8
1 : 4/8
2 : 1/8
>>> flips.mean
3/4
>>> P((flipA==1).given(flips<=1))
3/7
```

... to symbolic computation

```
>>> flipA = bernoulli('a')
>>> flipB = bernoulli('b')
>>> flips = flipA + flipB
>>> flips
0 : (a - 1)*(b - 1)
1 : -2*a*b + a + b
2 : a*b
>>> flips.mean
a + b
>>> P((flipA==1).given(flips<=1))
a*(b - 1)/(a*b - 1)
```

powered by  
[SymPy](#)

Jupyter Notebook session  
with automatic [LaTeX](#) rendering

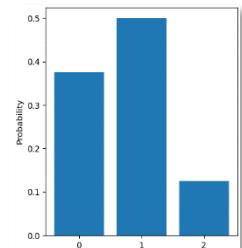
```
In [2]: x = binom(2, 'p')
y = binom(4, 'q')
z = x + y
P((y==2).given(z<=3,x>=1))
```

out[2]: 
$$\frac{12q^2(p-1)}{9pq^2 + 2pq + p - 6q^2 - 4q - 2}$$

## PP made easy!

```
>>> flipA = bernoulli(0.50)
>>> flipB = bernoulli(0.25)
>>> flips = flipA + flipB
>>> P(flipB == 0)
0.75
>>> flips
0 : 0.375
1 : 0.5
2 : 0.125
>>> flips.plot()
>>> P(flips <= 1)
0.875
>>> P((flips==0) | (flips==1))
0.875
>>> P((flipA==1) & (flips<=1))
0.375
>>> P(flipA==1) * P(flips<=1)
0.4375
>>> P((flipA==1).given(flips<=1))
0.42857142857142855
```

All operators are overloaded:  
+ - \* / < == & | ~ ...



0.375 ≠ 0.4375  
→ flipA and flips are interdependent!

conditional probability =  $\frac{0.375}{0.875}$

## A murder party (BN example)

```
>>> killer = pmf({ "Colonel Mustard": 0.60,
                     "Mrs. White" : 0.30,
                     "Mrs. Peacock" : 0.10 })
prior probabilities
```

if Mrs. White is the killer,  
then she's absent with prob. 90%  
else she's absent with prob. 20%

```
>>> mrs_white_is_absent = \
    if_( killer == "Mrs. White", event(0.90),
         event(0.20) )
```

if Mrs. Peacock is innocent,  
then she knows who's the killer  
with prob. 75%

```
>>> mrs_peacock_knows_who_is_killer = \
    if_( killer != "Mrs. Peacock", event(0.75),
         True )
```

if Mrs. Peacock is the killer  
or she knows who's the killer  
then she's absent with prob. 99%  
else she's absent with prob. 10%

```
>>> mrs_peacock_is_absent = \
    if_( (killer == "Mrs. Peacock") |
        mrs_peacock_knows_who_is_killer, event(0.99),
        event(0.10) )
```

Evidences:

1. Mrs. Peacock is absent.
2. Mrs White is present.
3. The killer is a woman.

```
>>> evidences = [ mrs_peacock_is_absent,
                  ~mrs_white_is_absent ,
                  killer[:4] == "Mrs." ]
Evidences: 1. Mrs. Peacock is absent.
2. Mrs White is present.
3. The killer is a woman.

>>> killer.given(*evidences)
Mrs. Peacock : 0.7747615553925166
Mrs. White   : 0.22523844460748343
```

